



Top partners: alternative scenarios



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Strong Dynamics at the Electroweak Scale
Montpellier, 7 December 2017



The uses or abuses of symmetries



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SM & hierarchy problems

d=0

$$\Lambda_{\text{UV}}^4 \sqrt{g}$$

d=2

$$c\Lambda_{\text{UV}}^2 |H|^2$$

d=4

$\mathcal{L}_{\text{kin}} + \text{gauge}$

$$Y_i^j \bar{\psi}_L^i H \psi_{Rj}$$

$$\lambda |H|^4$$

$$\theta \tilde{G}_{\mu\nu} \tilde{G}^{\mu\nu}$$

d>4

$$\frac{\lambda_M^{ij}}{\Lambda_{\text{UV}}} \ell_i H H \ell_j$$

$$\frac{\lambda_B}{\Lambda_{\text{UV}}^2} qqq\ell$$

$$\frac{e\hat{Y}_i^j}{\Lambda_{\text{UV}}^2} \bar{\psi}_L^i H \sigma^{\mu\nu} \psi_{Rj} F_{\mu\nu}$$

$$\frac{gg'}{\Lambda_{\text{UV}}^2} H^\dagger W_{\mu\nu} H B^{\mu\nu}$$

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$$\Lambda_{\text{UV}}^n$$

$$\Lambda_{\text{UV}}^\gamma$$

$$1/\Lambda_{\text{UV}}^n$$

Natural expectation gives rise to known hierarchy problems.

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tuning

$$m_H \ll \Lambda_{UV}$$

$$\Lambda_{UV}^\gamma$$

$$1/\Lambda_{UV}^n$$

Gauge principle + (unnatural) separation of scales describes observations.

SM accidental symmetries

$\Lambda_{UV} \gg \text{TeV}$, decoupling, explains a lot

	<u>symmetry</u>	<u>spurion</u>
<i>B, L numbers</i>	$U(1)_{B, L_e, L_\mu, L_\tau}$	“exact”
<i>Flavor</i>	$SU(3)_{q, u, d, \ell, e}$ $SU(2)_{\text{quarks}}^3$	$Y \rightarrow 0$ $y_t \neq 0$
<i>CP</i>	$\psi \rightarrow \psi^*$	$\delta \rightarrow 0$
<i>Custodial</i>	$SO(4)_C \cong SU(2)_L \times SU(2)_R$	$y_t, g' \rightarrow 0$
<i>Unification</i>	$SU(5)$	“remnant” $\bar{\mathbf{5}} + \mathbf{10}$

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hints of high UV scales

Gauge principle + (unnatural) decoupling has been “corroborated”:

neutrino masses?

$$m_\nu \approx 0.05\text{eV} \longleftrightarrow \frac{\lambda_M}{\Lambda_{\text{UV}}} \sim (10^{15}\text{GeV})^{-1}$$

$$\Lambda_{\text{UV}} \lesssim 10^7\text{GeV}$$

type I

strong CP problem?

$$\theta \ll 1 \longleftrightarrow \frac{a}{f_a} \tilde{G}_{\mu\nu} \tilde{G}^{\mu\nu}$$

$$\Lambda_{\text{UV}} \lesssim 4\pi f_a, f_a \gtrsim 10^9\text{GeV}$$

$$\Lambda_{\text{UV}} \lesssim 10\text{TeV}$$

KSVZ

dark matter?

$$(-1)^{3B+L+2s} = -1 \longleftrightarrow \text{“stability”}$$

Suggests the characteristic scale of *some* phenomena is high.

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We are not content with unnatural separation of scales:

$$\Lambda_{UV} \sim \text{TeV}$$

If no separation of scales, SM symmetries (successes) are generically lost.

&

No BSM physics discovered yet.



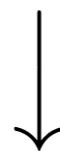
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BSM must enjoy SM **symmetries** (and **spurions**) at TeV energies.

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If **natural**, characteristic scale of *some* phenomena best kept high.



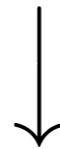
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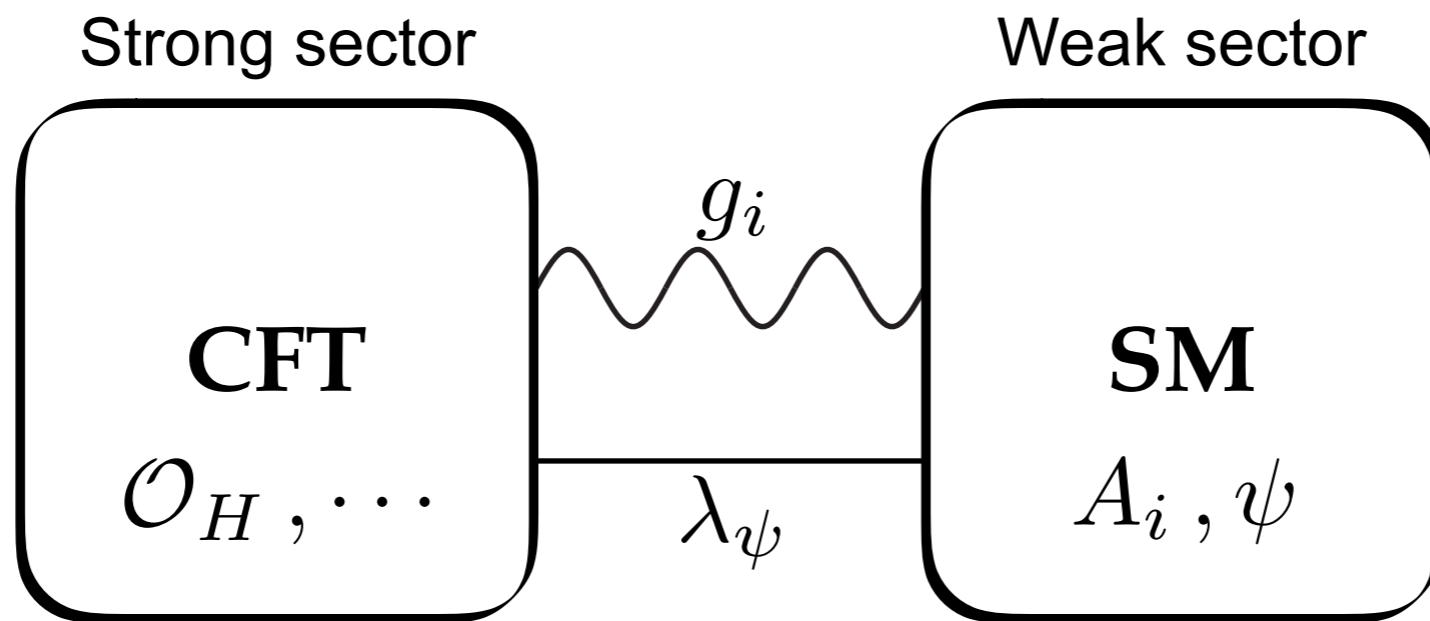
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Higgs (of course) and **top** are singled out:

$$\Lambda_{UV}^H \sim \Lambda_{UV}^t \sim \text{TeV}$$

modern Composite Higgs models

$$\Lambda'_{UV} \equiv \Lambda_{\mathcal{B}}, \Lambda_{\mathcal{L}}, \Lambda_{Flavor}, \Lambda_{S\psi(5)} ?$$



$d(\mathcal{O}_{|H|^2}) \gtrsim 4$ no more EW hierarchy problem

$$\Lambda_{UV}^H \equiv m_*$$

$g_* =$ Higgs coupling $g_* \gtrsim g_i, \lambda_\psi$

$f =$ Higgs scale

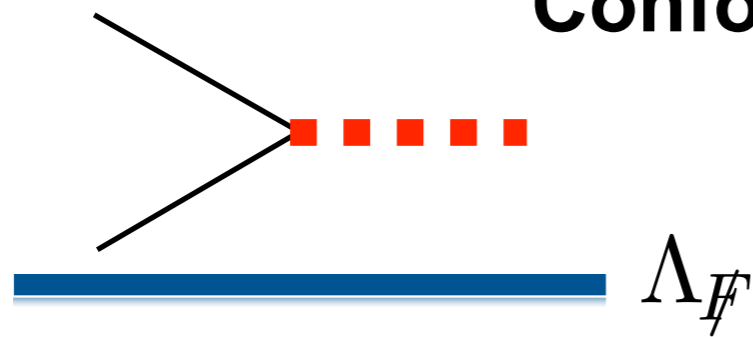
$m_* \sim g_* f =$ Composites' mass

$$\epsilon_{g_i} \equiv g_i/g_* \quad \epsilon_\psi \equiv \lambda_\psi/g_*$$

Energy

flavor generation & the top

Conformal Technicolor (CTC)



$$\frac{Y_i^j}{\Lambda_{\cancel{F}}^{d_H-1}} \bar{\psi}_L^i \mathcal{O}_H \psi_{Rj} + \frac{1}{\Lambda_{\cancel{F}}^2} \bar{\psi}^i \bar{\psi}^j \psi_k \psi_l$$

$$d_H = d(\mathcal{O}_H)$$

$$\text{Decoupling: } d_H \rightarrow 1, \Lambda_{\cancel{F}} \rightarrow \infty$$

$$d(\mathcal{O}_{|H|^2})$$

1 flavor spurion (SM):

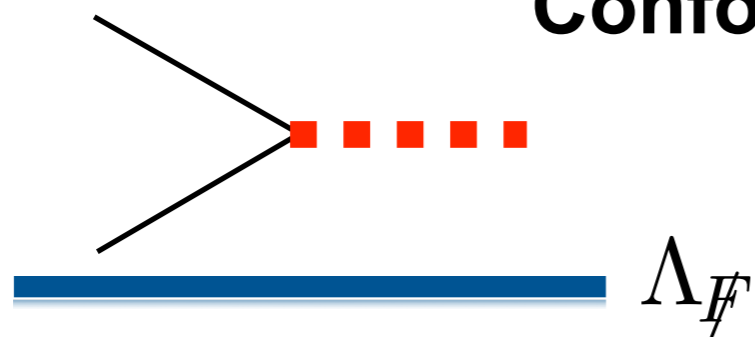
$$m_*$$

$$Y(m_*) \sim Y(\Lambda_{\cancel{F}}) \left(\frac{m_*}{\Lambda_{\cancel{F}}} \right)^{d_H-1}$$

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$$\begin{array}{c} \updownarrow \\ d(\mathcal{O}_{|H|^2}) \end{array}$$

1 flavor spurion (SM):

Diagram illustrating the energy level m_* . A red horizontal line represents the scale m_* .

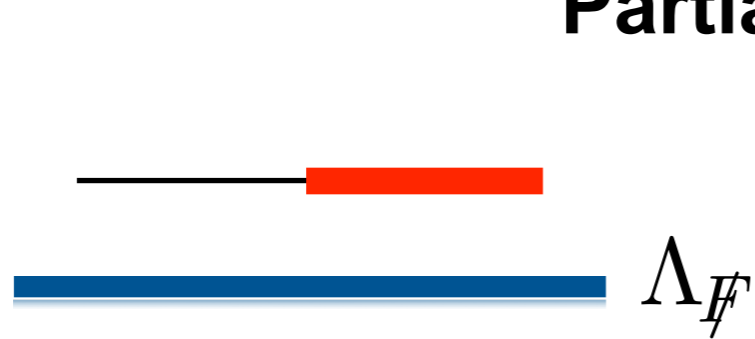
$$Y(m_*) \sim Y(\Lambda_{\cancel{F}}) \left(\frac{m_*}{\Lambda_{\cancel{F}}} \right)^{d_H-1}$$

top

$$y_t \sim 1 \longrightarrow \begin{array}{c} d_H \gtrsim 1.5 \\ \text{bootstrap} \\ d(\mathcal{O}_{|H|^2}) \gtrsim 4 \end{array} \longrightarrow \Lambda_{\text{UV}}^t \lesssim O(10)m_*$$

flavor generation & the top

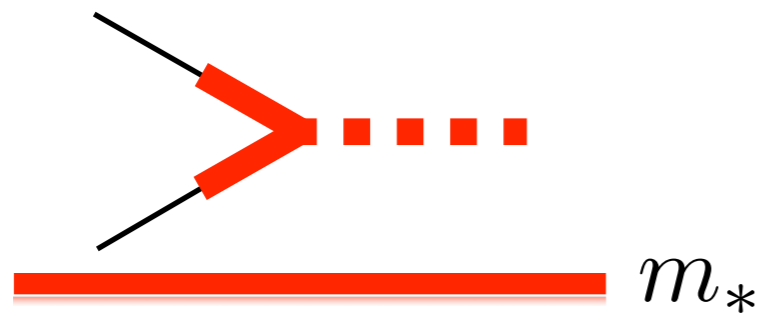
Partial Compositeness (PC)



$$\frac{g_* \epsilon_{\psi i}}{\Lambda_{\cancel{F}}^{d_\psi - 5/2}} \bar{\psi}^i \mathcal{O}_\psi + \frac{1}{\Lambda_{\cancel{F}}^2} \bar{\psi}^i \bar{\psi}^j \psi_k \psi_l$$

$$d_\psi = d(\mathcal{O}_\psi)$$

$$\text{Decoupling: } d_\psi \rightarrow 5/2, \Lambda_{\cancel{F}} \rightarrow \infty$$



2 flavor spurions:

$$\epsilon_{\psi_{L,R}}(m_*) \sim \epsilon_{\psi_{L,R}}(\Lambda_{\cancel{F}}) \left(\frac{m_*}{\Lambda_{\cancel{F}}} \right)^{d_{\psi_{L,R}} - 5/2}$$

flavor generation & the top

Partial Compositeness (PC)

$\Lambda_{\cancel{F}}$

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m_*

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top

$$y_t \sim \epsilon_q \epsilon_t g_* \sim 1 \longrightarrow \epsilon_{q,t} \in (y_t/g_*, 1) \longrightarrow \Lambda_{\text{UV}}^t \sim m_*$$

BSM (approximate) symmetries

B, L numbers

$U(1)_{B, L_e, L_\mu, L_\tau}$

e.g. neutrino masses

CTC

$$m_\tau \sim \frac{g_* v}{\sqrt{2}} \left(\frac{m_*}{\Lambda_{\cancel{F}}} \right)^{d_H - 1} \longrightarrow d_H \approx 2, \Lambda_{\cancel{F}} \approx 10^6 \text{ GeV}$$

$$m_\nu \sim \frac{(g_* v)^2}{2m_*} \left(\frac{m_*}{\Lambda_{\cancel{F}}} \right)^{2d_H - 1} \approx 10^5 (\Delta m)_{\text{atm}}$$

$$m_* = 3 \text{ TeV}, g_* = \pi$$

BSM (approximate) symmetries

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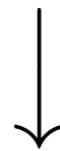
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We must require *L number* at $\Lambda_{\cancel{F}}$

use or abuse ?



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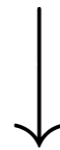
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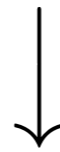
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Note that in PC *X number* must exist such that: $Y = T_R^3 + X$

$$X = \alpha L = \beta B$$

BSM (approximate) symmetries

Flavor & CP

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EDMs, $\mu \rightarrow e\gamma$, ϵ_K

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$$m_*^{\text{quarks}} \gtrsim 10\text{TeV}$$

$$m_*^{\text{leptons}} \gtrsim 100\text{TeV}$$

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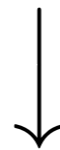
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We must require $SU(3)$ & CP symmetries at m_*

1 flavor spurion (SM): $\epsilon_{\psi_L} \sim Y$

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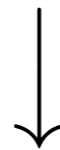
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Note dynamics (PC + CTC) can eliminate the need for accidental symmetries at m_*

BSM (approximate) symmetries

Custodial

$$SO(4)_C \cong SU(2)_L \times SU(2)_R$$

T-parameter

$$\frac{1}{f^2} |H^\dagger D_\mu H|^2 \quad \hat{T} \sim \frac{v^2}{f^2} \lesssim 10^{-3} \quad f \gtrsim 5\text{TeV}$$

Unavoidable *Custodial* symmetry at m_*

1-loop generated

use or abuse ?



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Unavoidable *Custodial* symmetry at m_*

1-loop generated



Custodial parity

$$P_{LR} : T_R^3(b_L) = T_L^3(b_L)$$

Zb_Lb_L coupling

$$\frac{\epsilon_q^2}{f^2} H^\dagger D_\mu H \bar{q} \gamma^\mu q \quad \delta g_b \sim \epsilon_q^2 \frac{v^2}{f^2} \lesssim 10^{-3} \quad m_* \gtrsim 4\text{TeV}$$

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Unavoidable *Custodial parity* at m_*

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1-loop generated

use or abuse ?



Custodial parity

$$P_{LR} : T_R^3(b_L) = T_L^3(b_L)$$

Zb_Lb_L coupling

$$\frac{\epsilon_q^2}{f^2} H^\dagger D_\mu H \bar{q} \gamma^\mu q \quad \delta g_b \sim \epsilon_q^2 \frac{v^2}{f^2} \lesssim 10^{-3} \quad m_* \gtrsim 4\text{TeV}$$

Unavoidable *Custodial parity* at m_*

1-loop generated

use or abuse ?



Note most CH models easily incorporate these symmetries; see next.

BSM (approximate) symmetries

Some effects cannot be suppressed by symmetries...

S-parameter

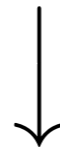
$$\frac{gg'}{m_*^2} H^\dagger W_{\mu\nu} H B^{\mu\nu} \quad \hat{S} \sim \epsilon_g^2 \frac{v^2}{f^2} \lesssim 10^{-3} \quad m_* \gtrsim 2.5 \text{ TeV}$$

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$$m_H \ll m_*$$

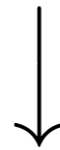
requires dynamics

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requires dynamics & symmetry

Higgs as a (pseudo-)NGB, $H \rightarrow H + f\theta$

use or abuse ?

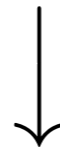


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Higgs as a (pseudo-)NGB, $H \rightarrow H + f\theta$

use or abuse ?



“Simple” extension of Technicolor idea:

e.g. $SO(5)/SO(4)$

with $SO(4)$ symmetry + P_{LR} automatic at LO in derivatives!

Higgs potential & top partners

$$V(H/f) = \epsilon_{\text{SM}}^2 \frac{m_*^4}{(4\pi)^2} \left(a \frac{|H|^2}{f^2} + \frac{b}{2} \frac{|H|^4}{f^4} \right)$$

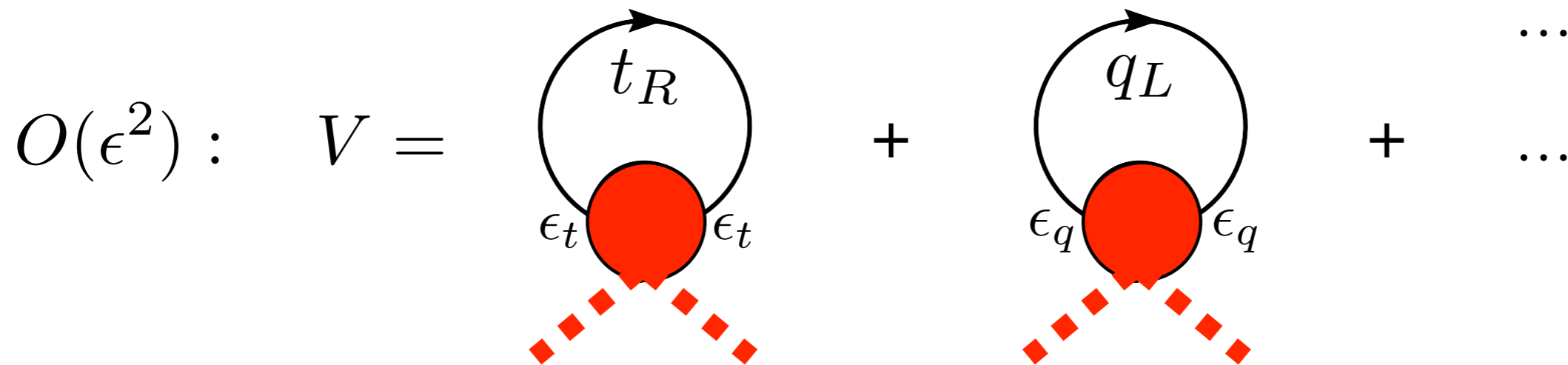
radiatively generated potential

spurions

$$\epsilon_t = \lambda_t / g_*$$

$$\epsilon_q = \lambda_q / g_*$$

$$\epsilon_g = g / g_*$$



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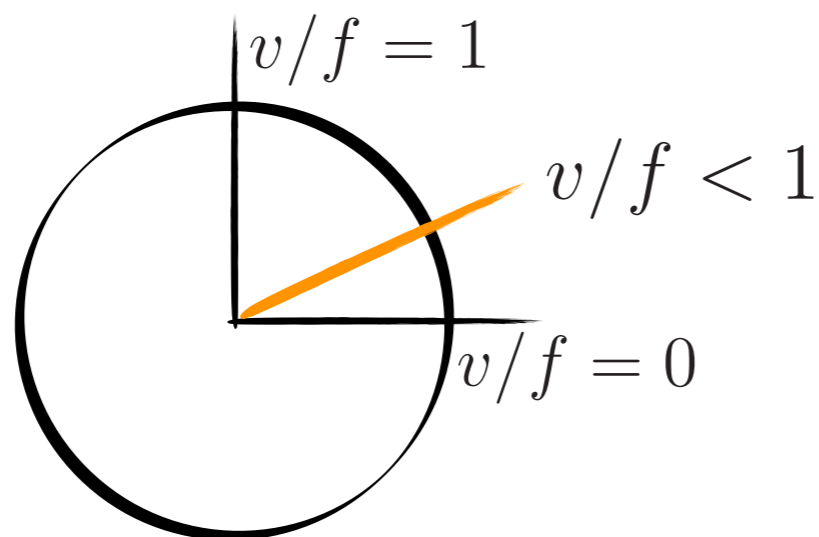
$$\epsilon_g = g / g_*$$

$$O(\epsilon^2) : \quad V = \text{[diagram: top loop]} + \text{[diagram: quark loop]} + \dots$$

The diagram shows two Feynman diagrams representing radiative corrections to the Higgs potential. The first diagram is a loop of a right-handed top quark (t_R) with a red circular vertex. Two external dashed red lines represent Higgs bosons, each labeled with a spurion ϵ_t . The second diagram is a loop of a left-handed quark (q_L) with a red circular vertex. Two external dashed red lines represent Higgs bosons, each labeled with a spurion ϵ_q . Ellipses indicate higher-order terms in the expansion.

Misalignment:

$$\frac{\langle H \rangle = v}{f} = \sqrt{\frac{a}{b}}$$



Higgs potential & top partners

$$V(H/f) = \epsilon_{\text{SM}}^2 \frac{m_*^4}{(4\pi)^2} \left(a \frac{|H|^2}{f^2} + \frac{b}{2} \frac{|H|^4}{f^4} \right)$$

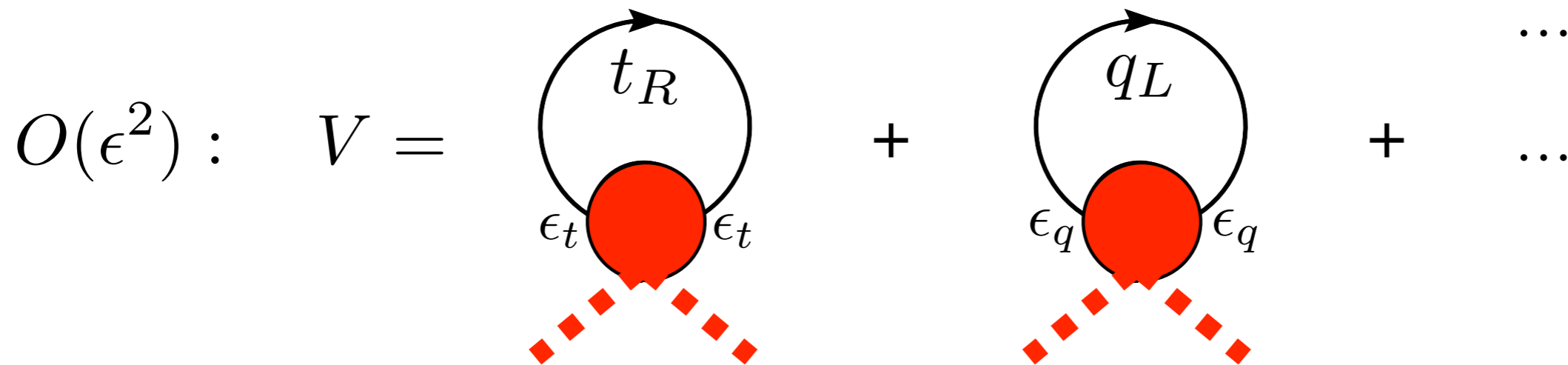
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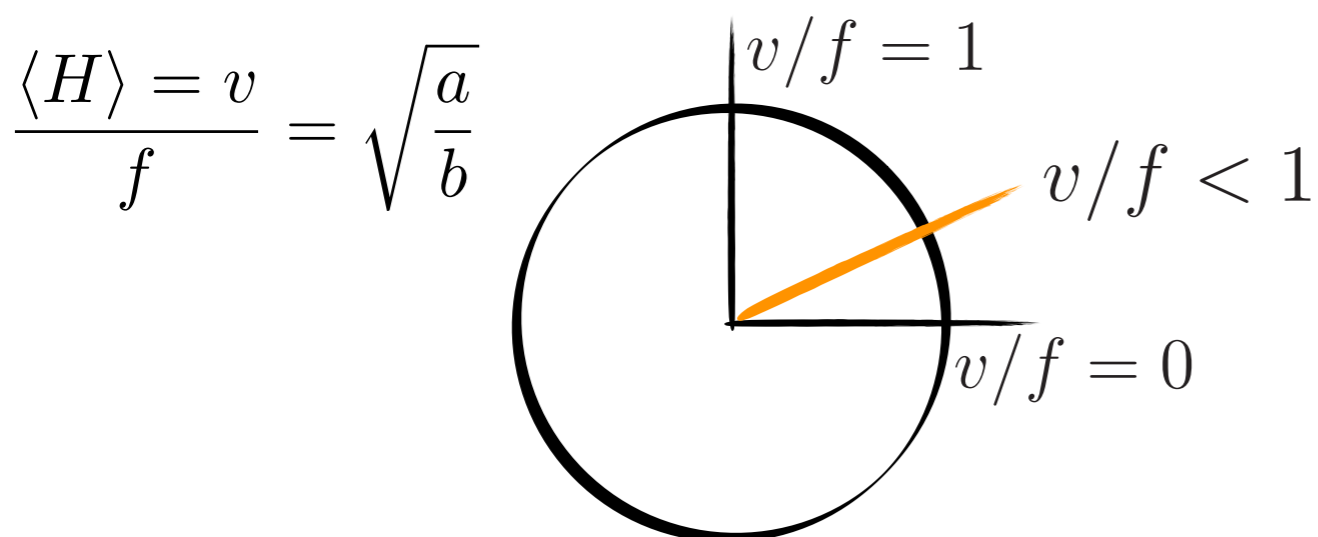
$$\epsilon_t = \lambda_t / g_*$$

$$\epsilon_q = \lambda_q / g_*$$

$$\epsilon_g = g / g_*$$



Misalignment:



Overall size:

$$\epsilon_{q,t} \in (y_t / g_*, 1) \text{ largest spurion}$$

$$V \sim \epsilon_{q,t}^2 \frac{m_T^4}{(4\pi^2)}$$

$m_* \rightarrow$ top partner's mass

Higgs potential & top partners

Top partners control the Higgs potential.

$$V_{\text{exp}} \approx -\frac{m_h^2}{2}|H|^2 + \frac{m_h^2}{2v^2}|H|^4 \quad \begin{array}{l} m_h \approx 125\text{GeV} \\ v \approx 246\text{GeV} \end{array}$$

reproduced only if **light & weakly coupled top partners**:

$$\Delta_{\mu^2} \sim (0.1)^{-1} \left(\frac{\lambda_{q,t}^2}{3y_t^2} \right) \left(\frac{m_T}{1\text{TeV}} \right)^2 \quad \Delta_{\lambda} \sim (1)^{-1} \left(\frac{\lambda_{q,t}^2}{3y_t^2} \right) \left(\frac{g_T}{2} \right)^2$$

$g_T = m_T/f$

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$g_T = m_T/f$

and a *mild tuning*.

Higgs couplings

$$\frac{1}{f^2} (\partial_\mu |H|^2)^2 \quad \delta g_h \sim \frac{v^2}{f^2} \lesssim 0.1 \quad f \gtrsim 750\text{GeV}$$

top partners phenomenology

Phenomenology dictated by **quantum numbers**:

$$SU(3)_C \times [SO(5)/SU(2)_L \times SU(2)_R] \times U(1)_X$$

$$\mathbf{5} = (\mathbf{1}, \mathbf{1}) \oplus (\mathbf{2}, \mathbf{2})$$

$$\Psi_1 = (\mathbf{3}, \mathbf{1}, \mathbf{1})_{2/3}$$

$$\Psi_4 = (\mathbf{3}, \mathbf{2}, \mathbf{2})_{2/3}$$

...

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QCD double production:

$$p(g)p(g) \rightarrow \Psi\bar{\Psi}$$

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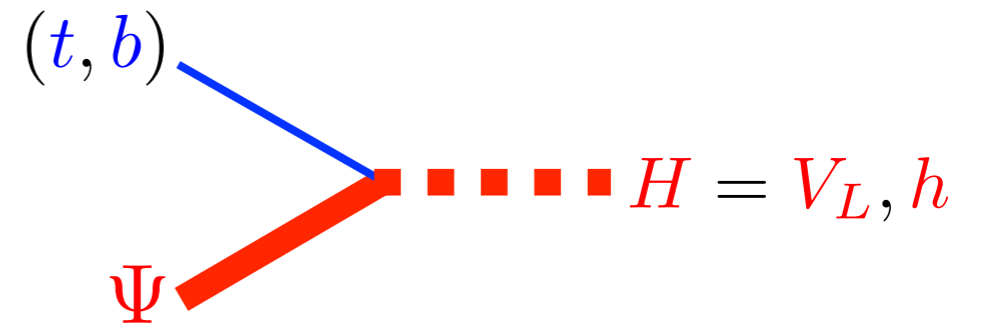
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$$p(V_L) p(t, b) \rightarrow \Psi + j(\bar{t}, \bar{b})$$

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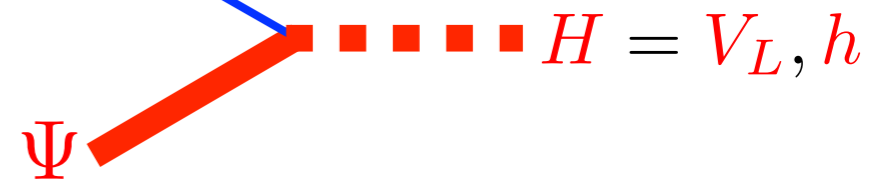
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...

(t, b)



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Branching ratios:

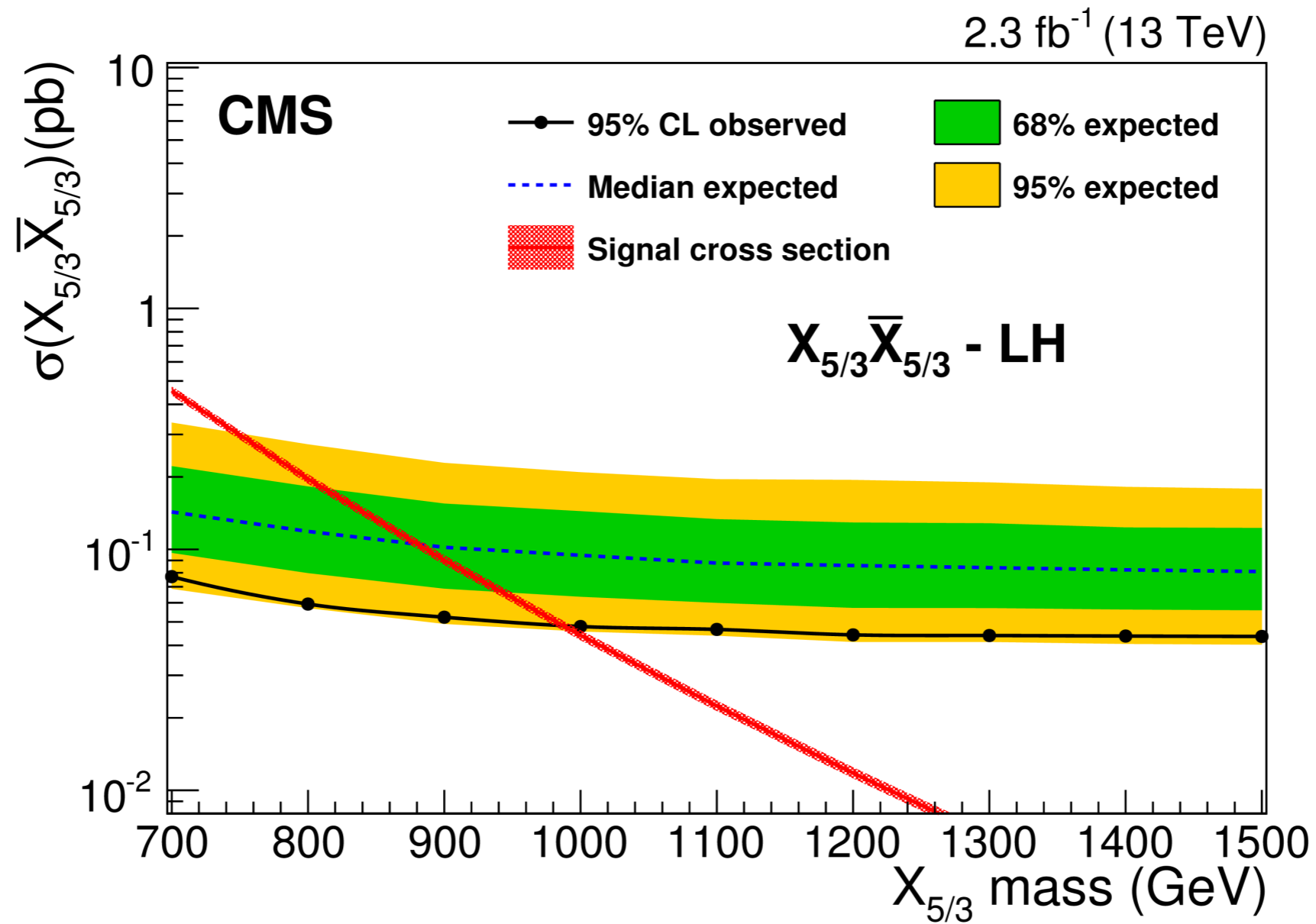
$$\Psi_1 \rightarrow (h, Z_L) t, W_L^+ b$$

$$T \rightarrow (h, Z_L) t$$

$$X_{5/3} \rightarrow W_L^+ t$$

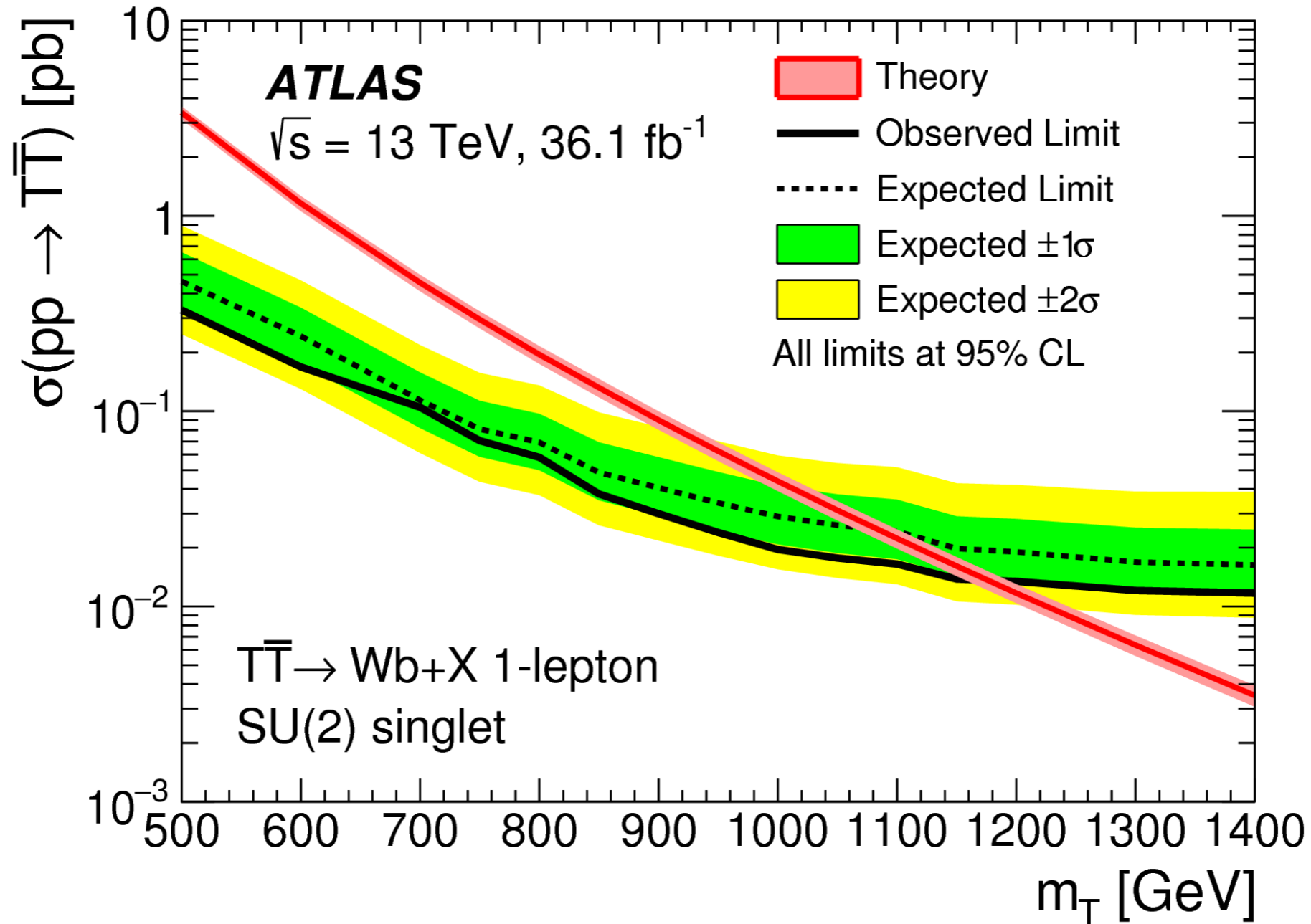
where are the top partners?

LHC 13TeV data



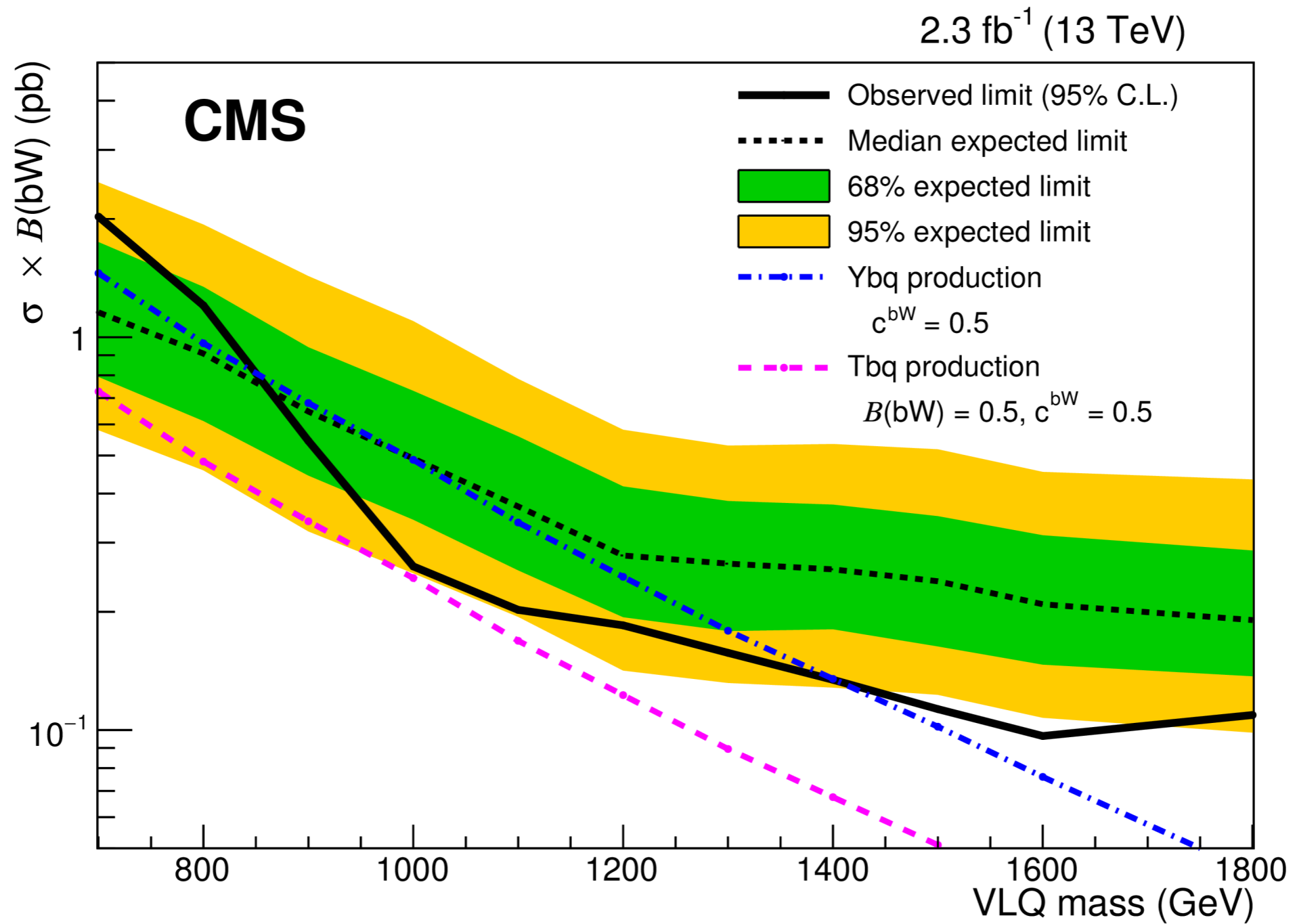
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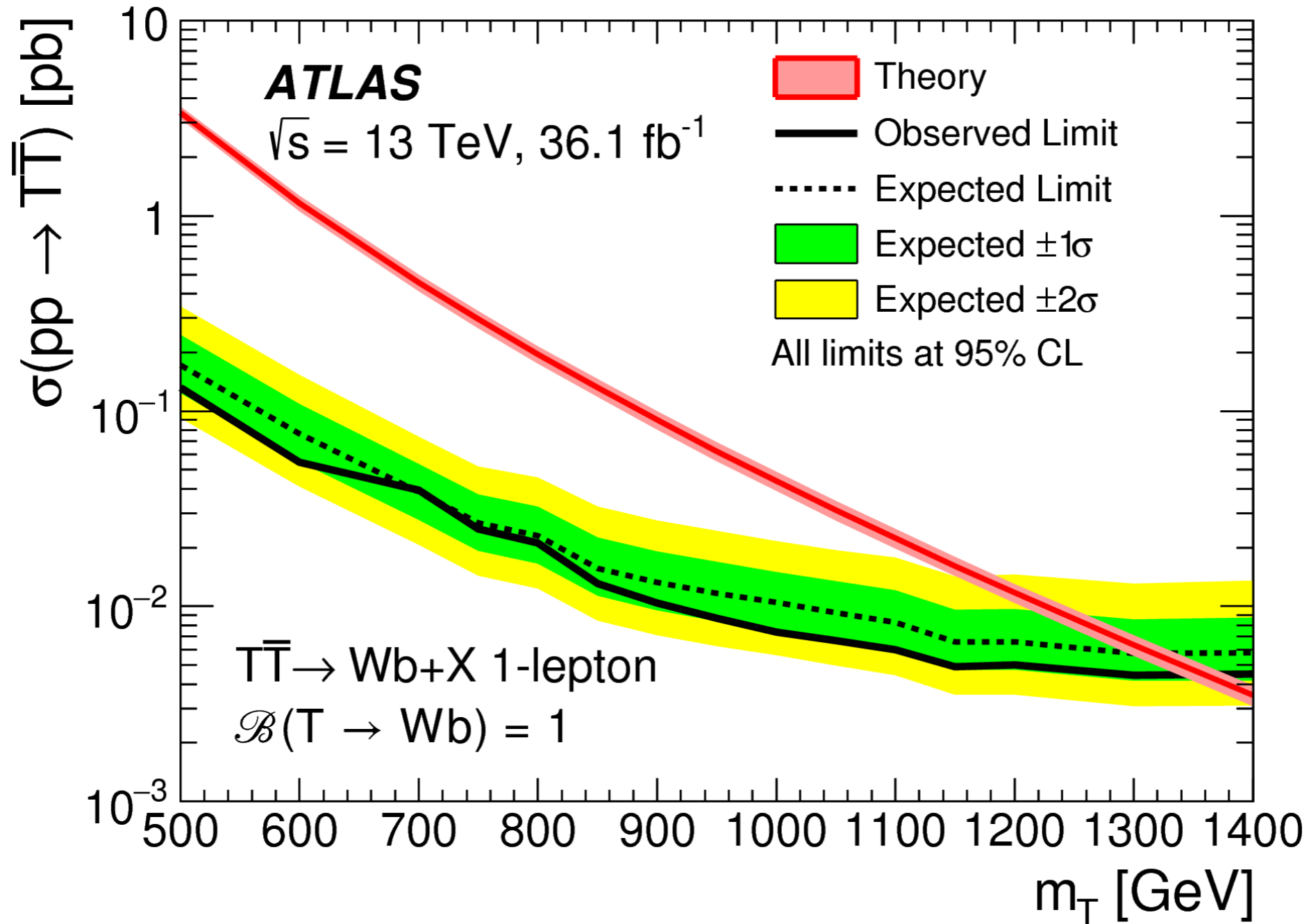
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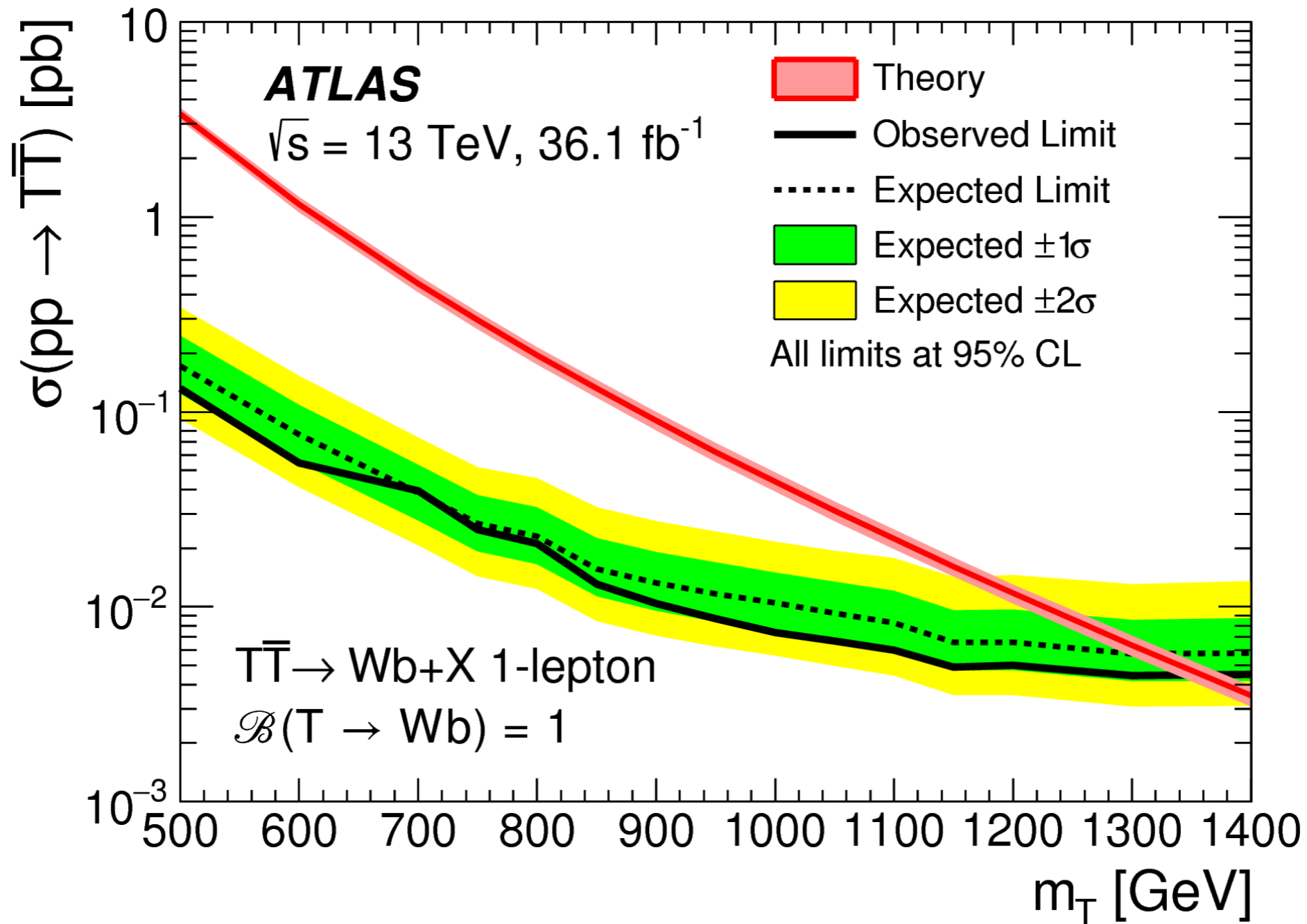
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LHC 13TeV data



where are the top partners?

LHC 13TeV data



$$m_T \gtrsim 1.35 \text{ TeV} \longrightarrow \Delta \sim (0.05)^{-1}$$

Increased tuning from LHC searches.

more BSM (approximate) symmetries

What if there are **non-standard** top-partner decays.

e.g. $SO(6)/SO(5)$

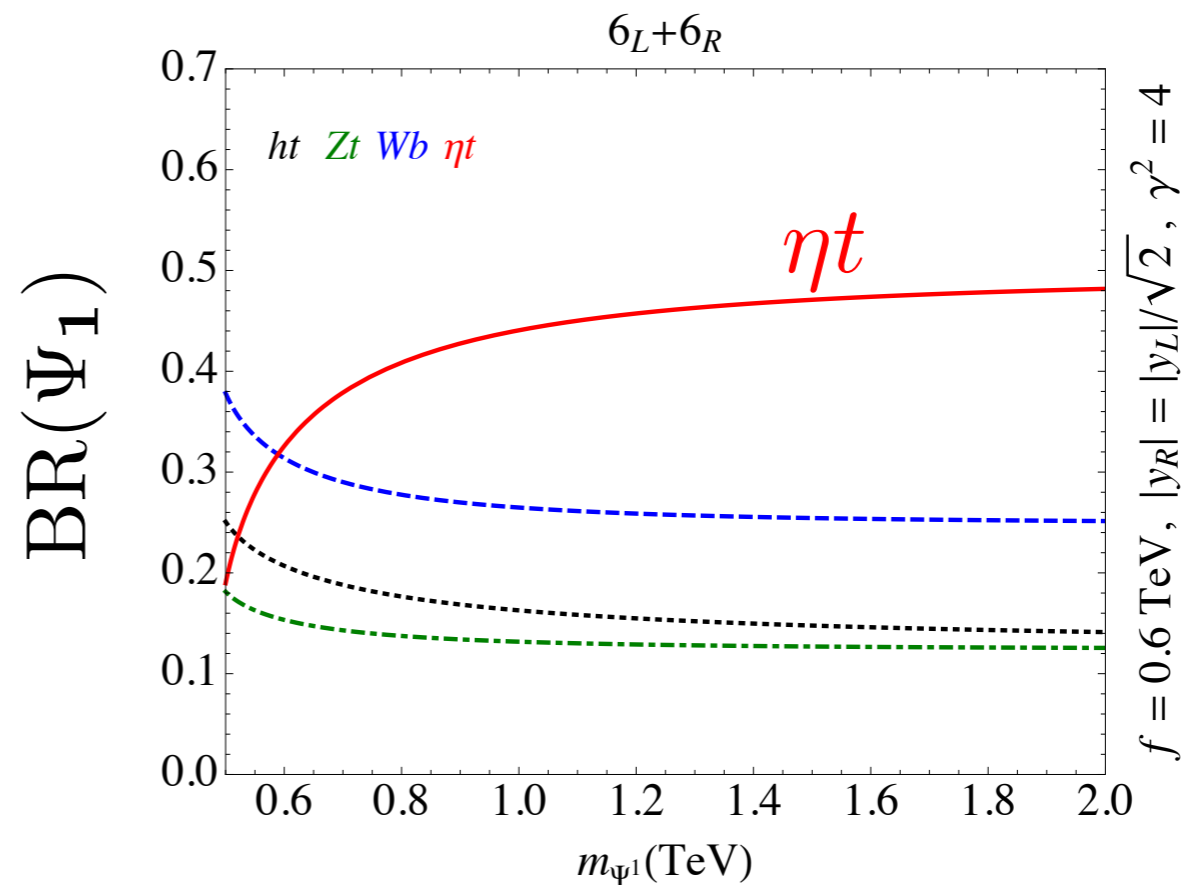
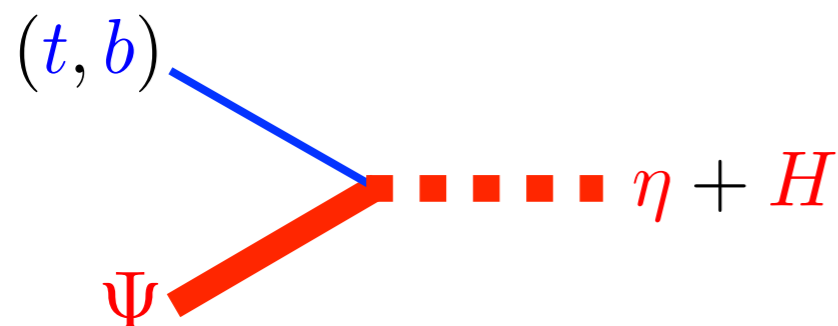
One extra singlet NGB beyond the Higgs:

$$\mathbf{5} = \eta + H = (\mathbf{1}, \mathbf{1}) \oplus (\mathbf{2}, \mathbf{2})_{SU(2)_L \times SU(2)_R}$$

η naturally light:

$$m_\eta \sim \epsilon_{q,t} \frac{g_T}{4\pi} m_T < m_T$$

η coupled to Ψ :



$m_\eta = 300 \text{ GeV}$

more BSM (approximate) symmetries

What if there are **non-standard top-partner decays**.

e.g. $SO(6)/SO(5)$

use or abuse ?



Note this is the minimal CH model with $SO(4)_C$ realizable à la QCD (technifermions).

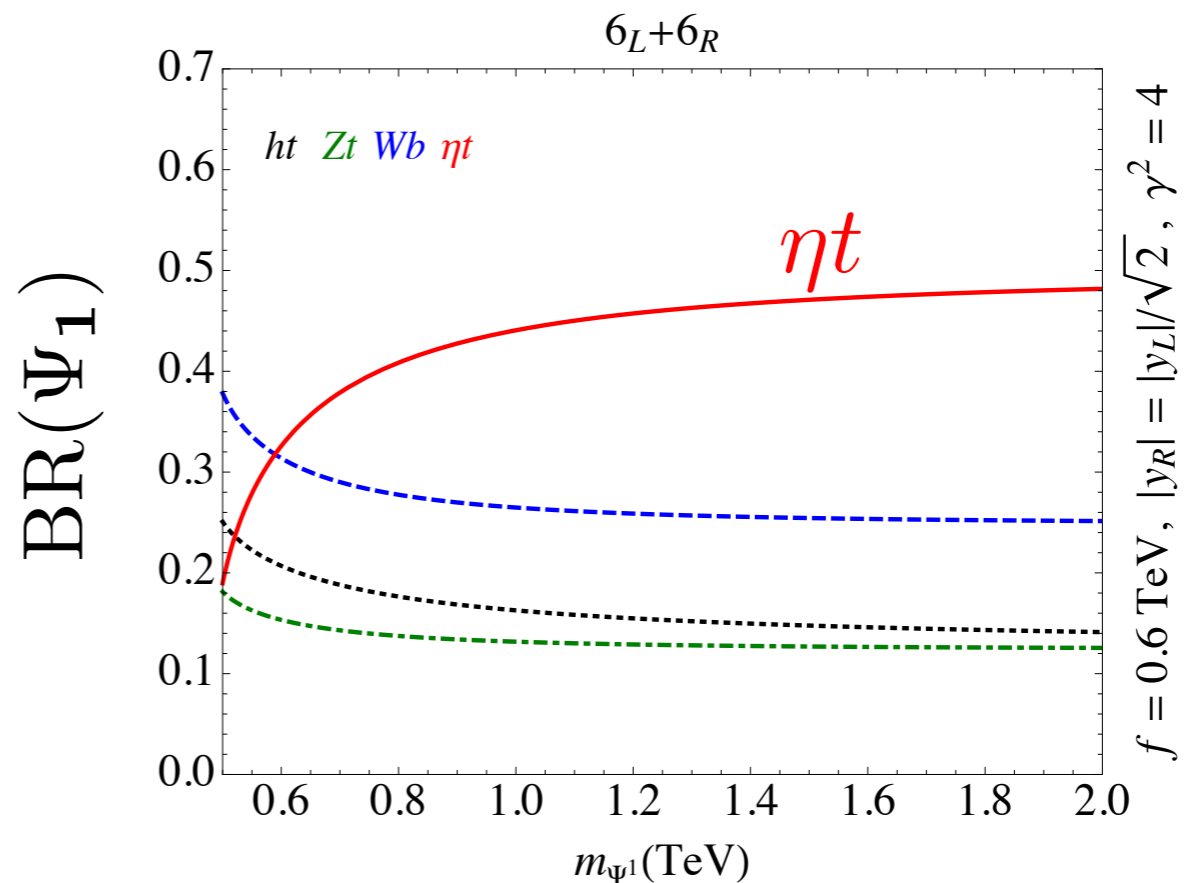
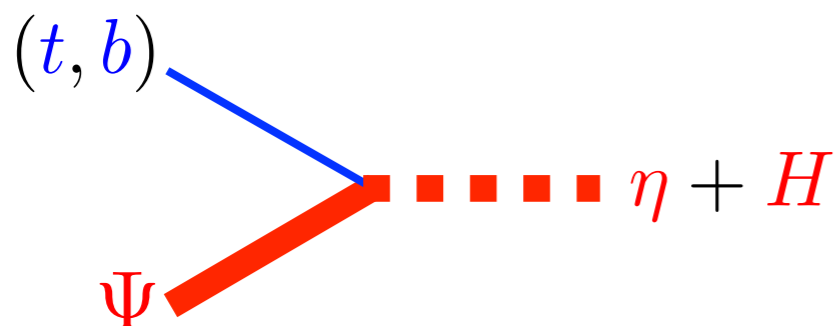
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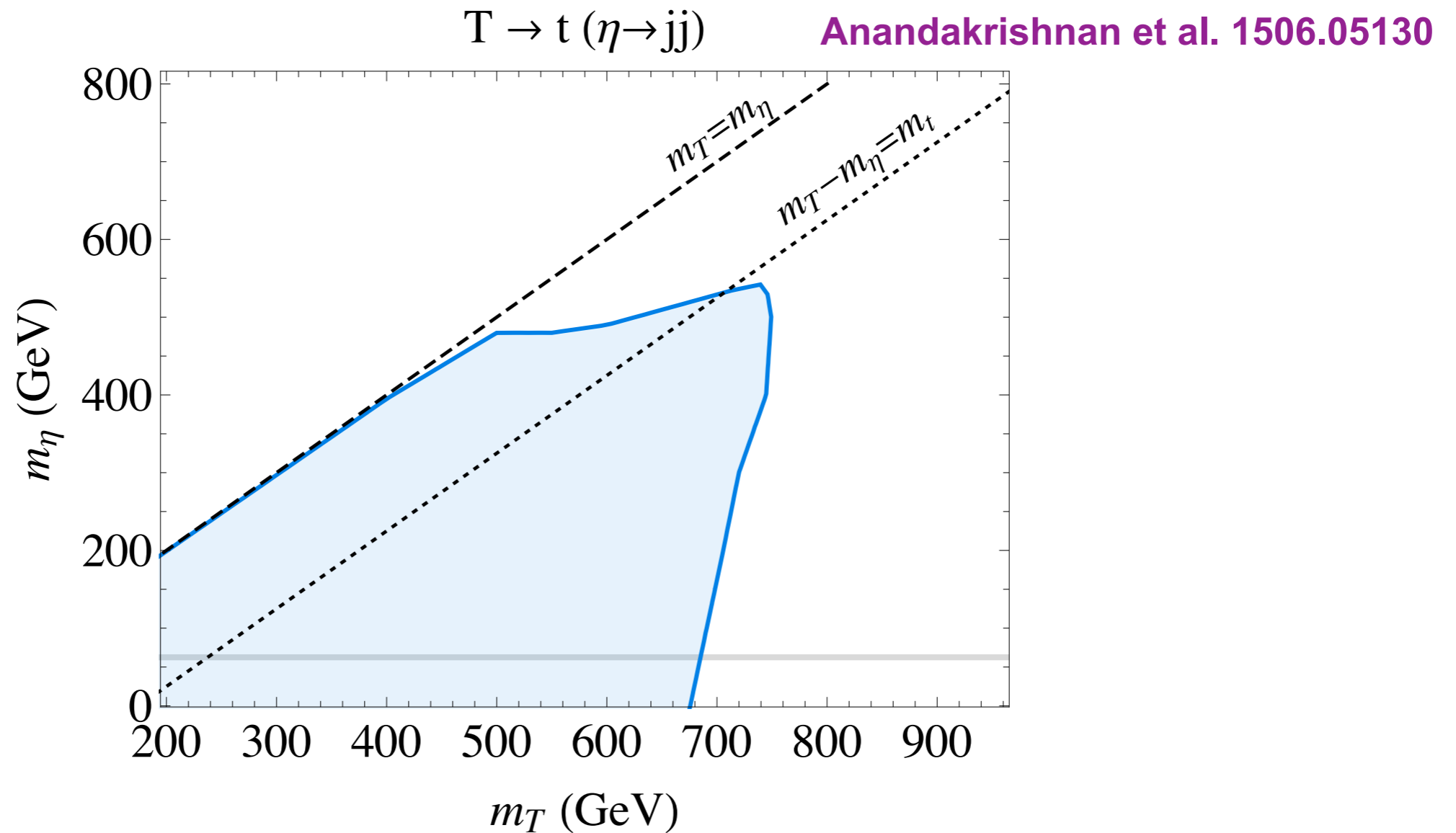


$m_\eta = 300$ GeV

more BSM (approximate) symmetries

$$\text{BR}(\eta \rightarrow gg) \approx 1 \quad \text{if} \quad m_\eta \lesssim 2m_t$$

(recast of) LHC 8TeV data

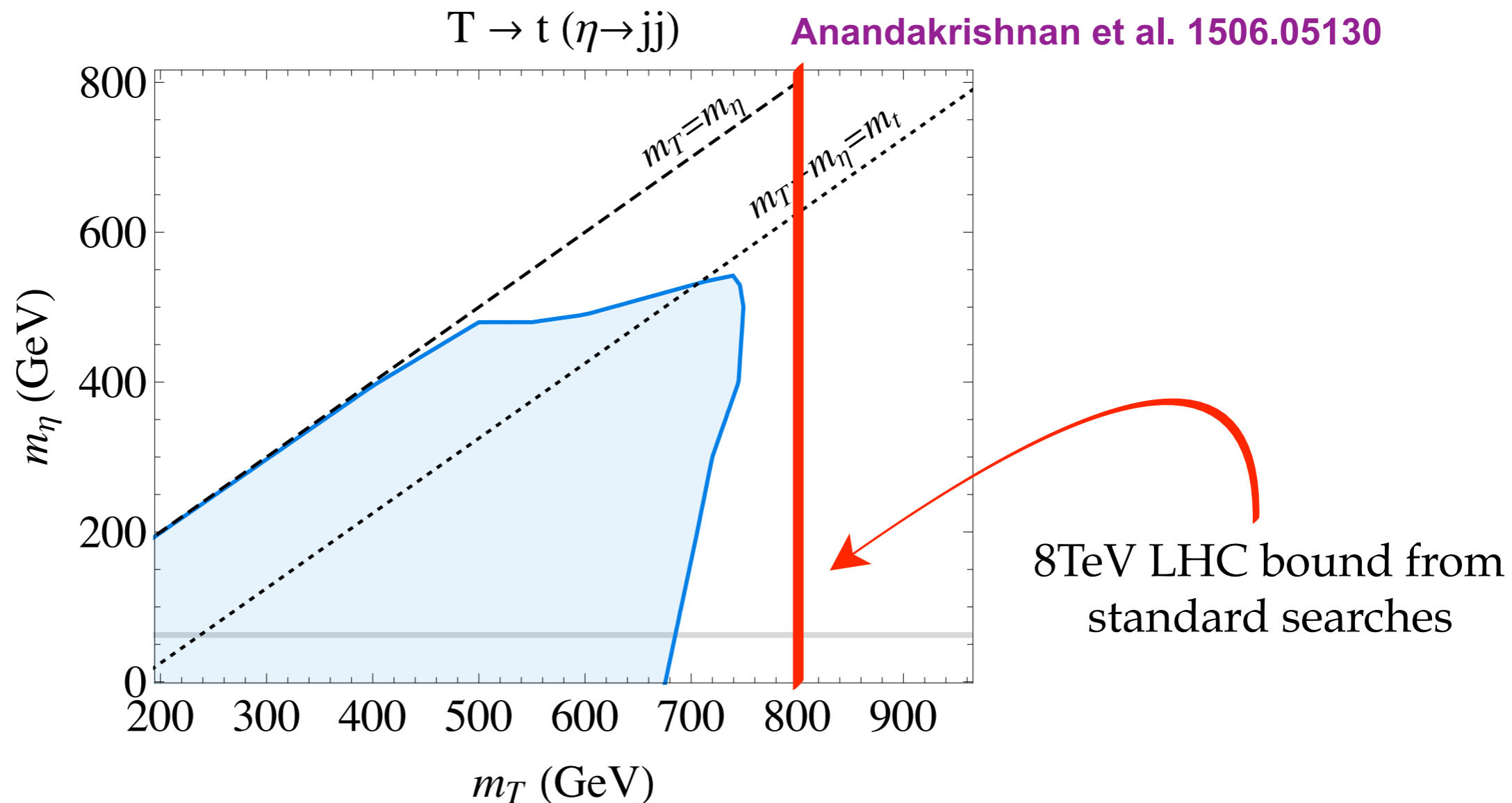


The bounds, thus tuning, are *mildly* weaker.

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(recast of) LHC 8TeV data



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Are *colored* top partners really needed?

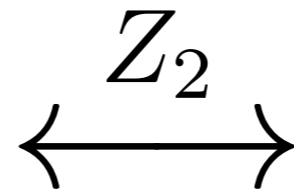
Twin Higgs mechanism

SM



gauged

$$SU(3)_C \times SU(2)_L \times U(1)_Y$$



$\widetilde{\text{SM}}$



gauged

$$\widetilde{SU(3)}_C \times \widetilde{SU(2)}_L \times \widetilde{U(1)}_Y$$

$$V(H, \widetilde{H}) = -\mu^2 \left(|H|^2 + |\widetilde{H}|^2 \right) + \frac{\lambda}{4} \left(|H|^2 + |\widetilde{H}|^2 \right)^2 + \dots$$

the last epicycle on BSM (approximate) symmetries

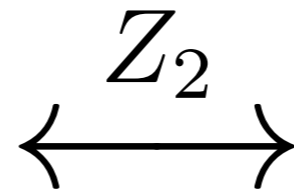
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$\widetilde{\text{SM}}$



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$$SU(3)_C \times SU(2)_L \times U(1)_Y$$

gauged

$$\widetilde{SU}(3)_C \times \widetilde{SU}(2)_L \times \widetilde{U}(1)_Y$$

$$V(H, \widetilde{H}) = -\mu^2 \left(|H|^2 + |\widetilde{H}|^2 \right) + \frac{\lambda}{4} \left(|H|^2 + |\widetilde{H}|^2 \right)^2 + \dots$$

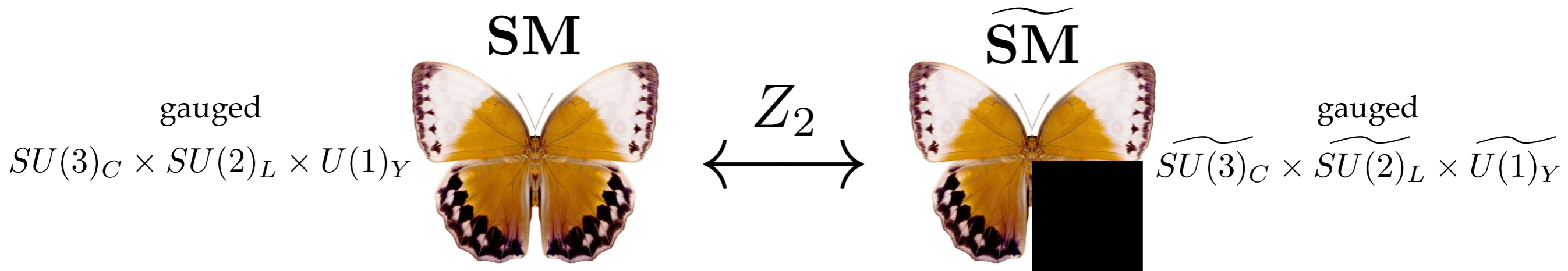
$$V_{LO} = \text{[diagram with } H \text{ and } y_t \text{]} + \text{[diagram with } \widetilde{H} \text{ and } \widetilde{y}_t \text{]} \quad y_t = \widetilde{y}_t$$

The diagram shows two Feynman diagrams for the leading order potential V_{LO} . The first diagram features a red dashed line labeled H connecting two red circular vertices labeled y_t . These vertices are connected by two curved arrows: the top one is labeled t_R and the bottom one is labeled q_L . The second diagram is identical but uses tilded variables: a red dashed line labeled \widetilde{H} connects two red circular vertices labeled \widetilde{y}_t , with curved arrows labeled \widetilde{t}_R and \widetilde{q}_L . To the right of the diagrams, the text $y_t = \widetilde{y}_t$ is written.

the last epicycle on BSM (approximate) symmetries

Are *colored* top partners really needed?

Twin Higgs mechanism



$$V(H, \tilde{H}) = -\mu^2 \left(|H|^2 + |\tilde{H}|^2 \right) + \frac{\lambda}{4} \left(|H|^2 + |\tilde{H}|^2 \right)^2 + \dots$$

$$V_{LO} = \text{---} H \text{---} \begin{array}{c} \text{---} t_R \text{---} \\ \text{---} y_t \text{---} \\ \text{---} q_L \text{---} \end{array} \text{---} + \text{---} \tilde{H} \text{---} \begin{array}{c} \text{---} \tilde{t}_R \text{---} \\ \text{---} \tilde{y}_t \text{---} \\ \text{---} \tilde{q}_L \text{---} \end{array} \text{---} \quad y_t = \tilde{y}_t$$

$$\langle H \rangle = 0, \langle \tilde{H} \rangle = f/\sqrt{2} \quad \downarrow$$

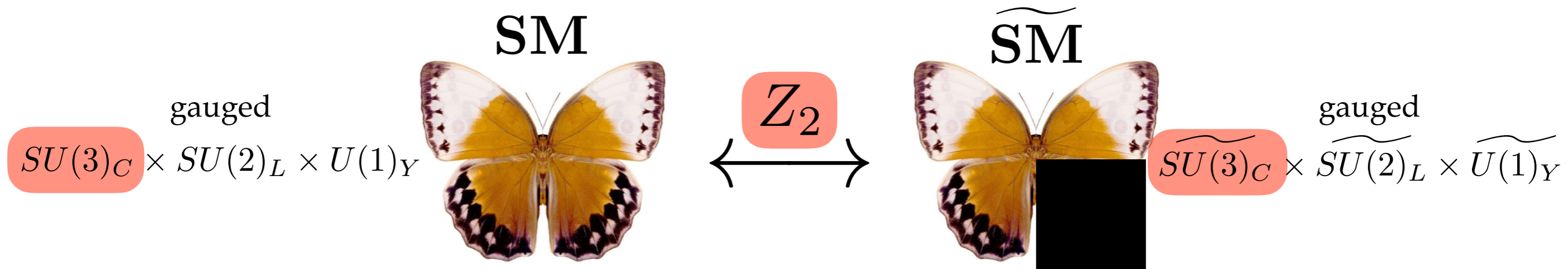
$$SO(8)/SO(7)$$

The Higgs is an exact NGB, even after radiative corrections!

the last epicycle on BSM (approximate) symmetries

Are colored top partners really needed?

Twin Higgs mechanism



$$V(H, \tilde{H}) = -\mu^2 \left(|H|^2 + |\tilde{H}|^2 \right) + \frac{\lambda}{4} \left(|H|^2 + |\tilde{H}|^2 \right)^2 + \dots$$

$$V_{LO} = \text{diagram with } H \text{ and } y_t \text{ loops} + \text{diagram with } \tilde{H} \text{ and } \tilde{y}_t \text{ loops} \quad y_t = \tilde{y}_t$$

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use or abuse ?

$$SO(8)/SO(7)$$



The Higgs is an exact NGB, even after radiative corrections!

twin Higgs

How do we get the Higgs VEV & mass?

$$V(H, \tilde{H}) = -\mu^2 \left(|H|^2 + |\tilde{H}|^2 \right) + \frac{\lambda}{4} \left(|H|^2 + |\tilde{H}|^2 \right)^2 + \frac{\hat{\lambda}}{8} \left(|H|^4 + |\tilde{H}|^4 \right)$$

$SO(4) \times \widetilde{SO(4)}$

$$V_{NLO} = \text{[diagram 1]} + \text{[diagram 2]} \quad y_t = \tilde{y}_t$$

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$SO(4) \times \widetilde{SO(4)}$

$$V_{NLO} = \text{---} H \text{---} \begin{array}{c} \text{---} \\ \circ y_t \\ \text{---} \\ \circ y_t \\ \text{---} \\ \circ y_t \\ \text{---} \\ \circ y_t \\ \text{---} \\ \circ y_t \\ \text{---} \\ \text{---} \end{array} \text{---} + \text{---} \tilde{H} \text{---} \begin{array}{c} \text{---} \\ \circ \tilde{y}_t \\ \text{---} \\ \circ \tilde{y}_t \\ \text{---} \\ \circ \tilde{y}_t \\ \text{---} \\ \circ \tilde{y}_t \\ \text{---} \\ \text{---} \end{array} \text{---} \quad y_t = \tilde{y}_t$$

$$SO(8)/SO(7) \downarrow \Sigma = \begin{pmatrix} H & & & & & & & \tilde{H} \\ \pi_1 & \pi_2 & \pi_3 & h & \tilde{\pi}_1 & \tilde{\pi}_2 & \tilde{\pi}_3 & \sqrt{1 - \pi_i^2 + \tilde{\pi}_i^2 - h^2} \end{pmatrix}$$

twin Higgs

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$$V_{NLO} = \text{[diagram with } H \text{ and } y_t \text{]} + \text{[diagram with } \tilde{H} \text{ and } \tilde{y}_t \text{]} \quad y_t = \tilde{y}_t$$

$$SO(8)/SO(7) \downarrow \Sigma = \left(\begin{array}{c} H \\ \pi_1 \ \pi_2 \ \pi_3 \ h \end{array} \right) \left(\begin{array}{c} \tilde{H} \\ \tilde{\pi}_1 \ \tilde{\pi}_2 \ \tilde{\pi}_3 \ \sqrt{1 - \pi_i^2 + \tilde{\pi}_i^2 - h^2} \end{array} \right)$$

twin Higgs

How do we get the Higgs VEV & mass?

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twin Higgs

How do we get the Higgs VEV & mass?

$$V(H, \tilde{H}) = -\mu^2 \left(|H|^2 + |\tilde{H}|^2 \right) + \frac{\lambda}{4} \left(|H|^2 + |\tilde{H}|^2 \right)^2 + \frac{\hat{\lambda}}{8} \left(|H|^4 + |\tilde{H}|^4 \right)$$

$SO(4) \times \widetilde{SO(4)}$

$$V_{NLO} = \text{[diagram with } H \text{ and } y_t \text{]} + \text{[diagram with } \tilde{H} \text{ and } \tilde{y}_t \text{]} \quad y_t = \tilde{y}_t$$

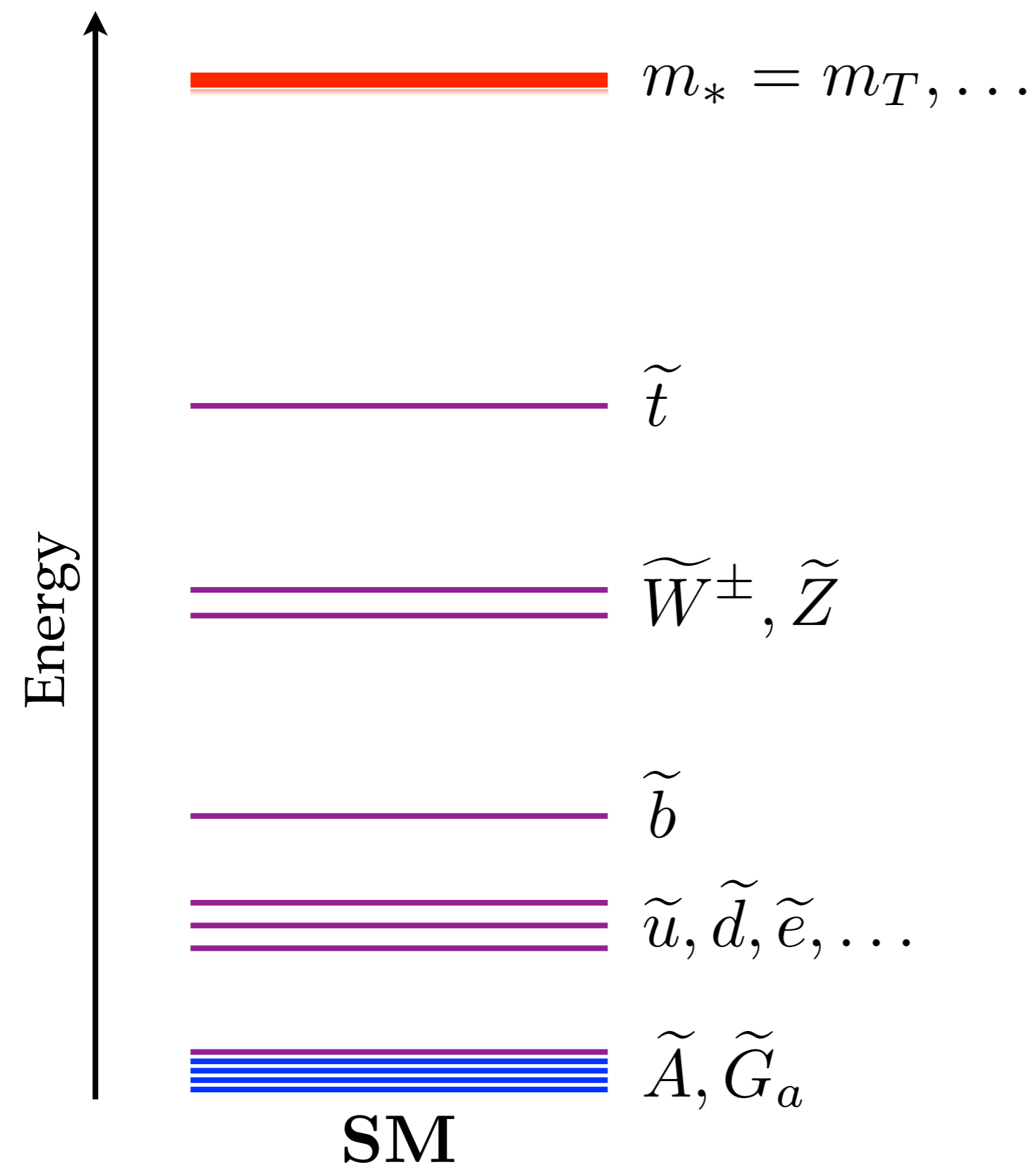
$$SO(8)/SO(7) \downarrow \Sigma = \left(\begin{array}{c} H \\ \pi_1 \ \pi_2 \ \pi_3 \ h \end{array} \left| \begin{array}{c} \tilde{H} \\ \cancel{\tilde{\pi}_1} \ \cancel{\tilde{\pi}_2} \ \cancel{\tilde{\pi}_3} \ \sqrt{1 - \pi_i^2 + \cancel{\tilde{\pi}_i^2} - h^2} \end{array} \right. \right)$$

$$V(H) = \frac{3f^4}{64\pi^2} \left[y_t^4 |H|^2 + \tilde{y}_t^4 (1 - |H|^2)^2 \right] \log \quad y_t = \tilde{y}_t$$

The Higgs potential is not sensitive to (colored) top partner mass.
There is no tension (tuning) coming from LHC searches.

twin Higgs

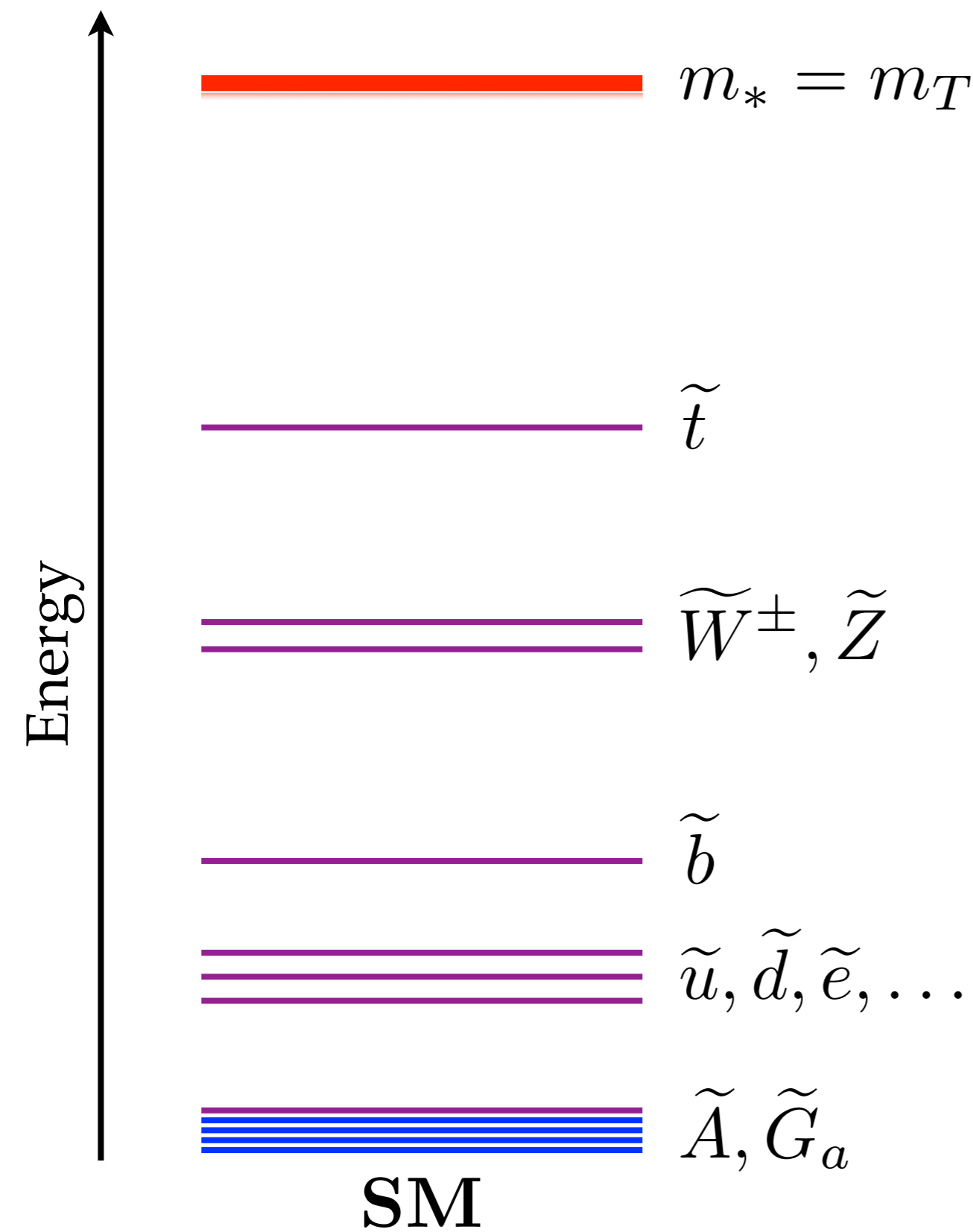
$$\langle H \rangle = 0$$



$$m_{\tilde{\psi}} = \frac{y_\psi f}{\sqrt{2}}$$
$$m_{\tilde{W}} = \frac{gf}{2}$$

twin Higgs

$$\langle H \rangle = 0$$



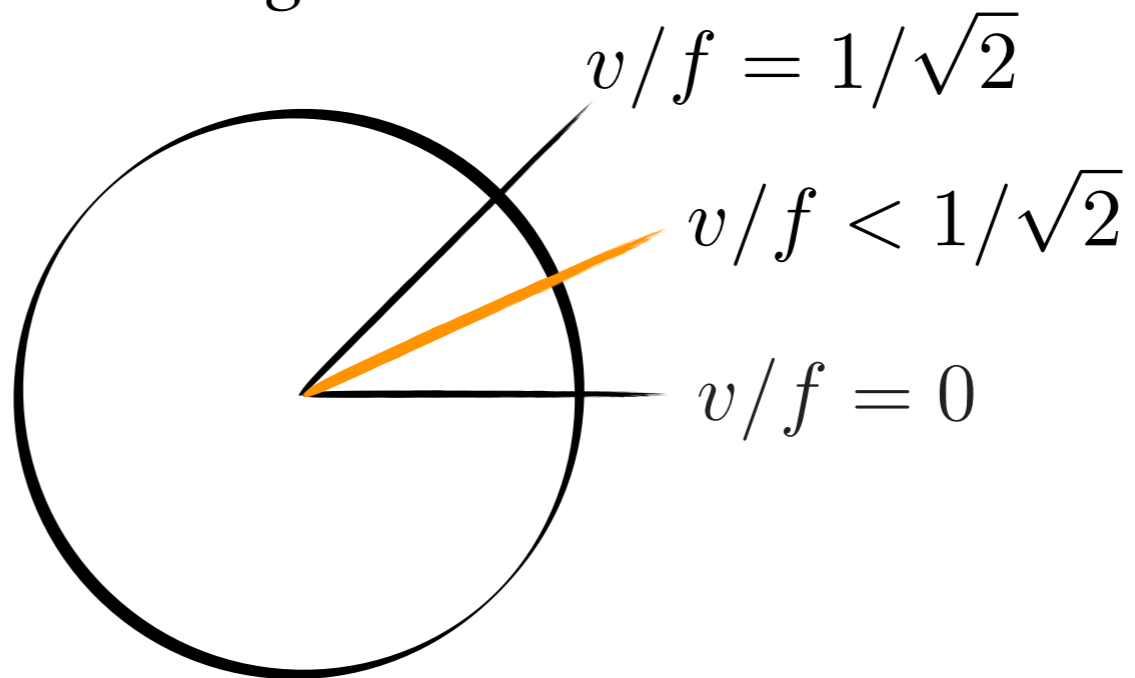
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All twin states are SM-neutral.

twin Higgs

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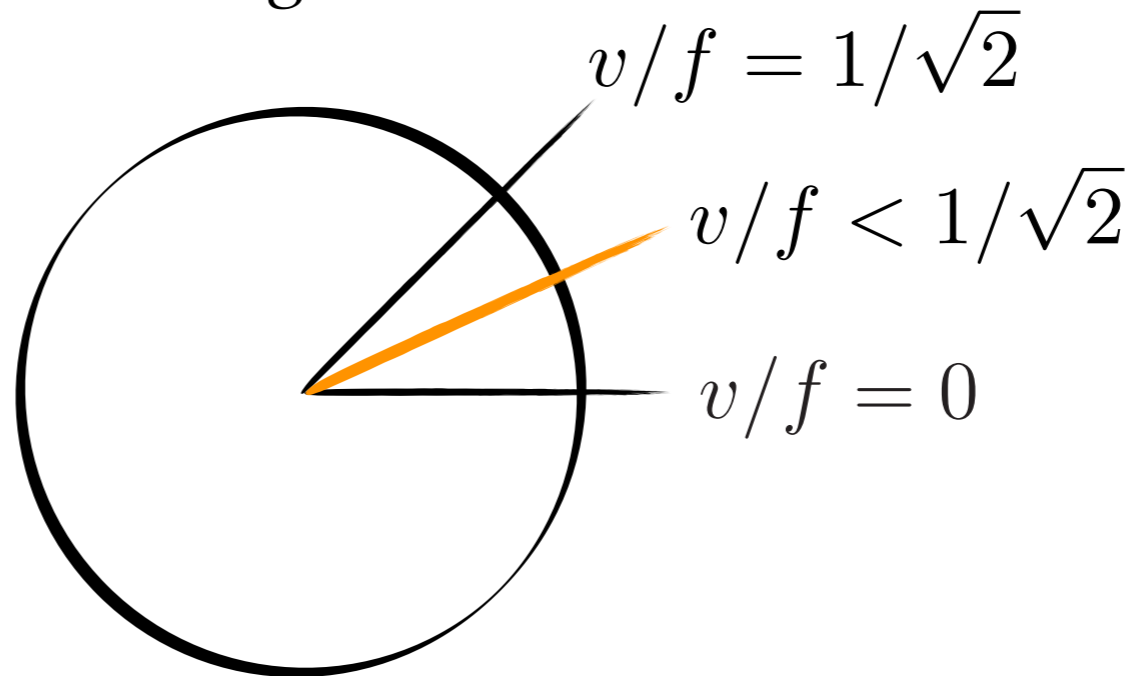
Misalignment:



twin Higgs

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Misalignment:



Minimal **tuning**:

$$\Delta_v^{-1} = 2 \frac{v^2}{f^2}$$

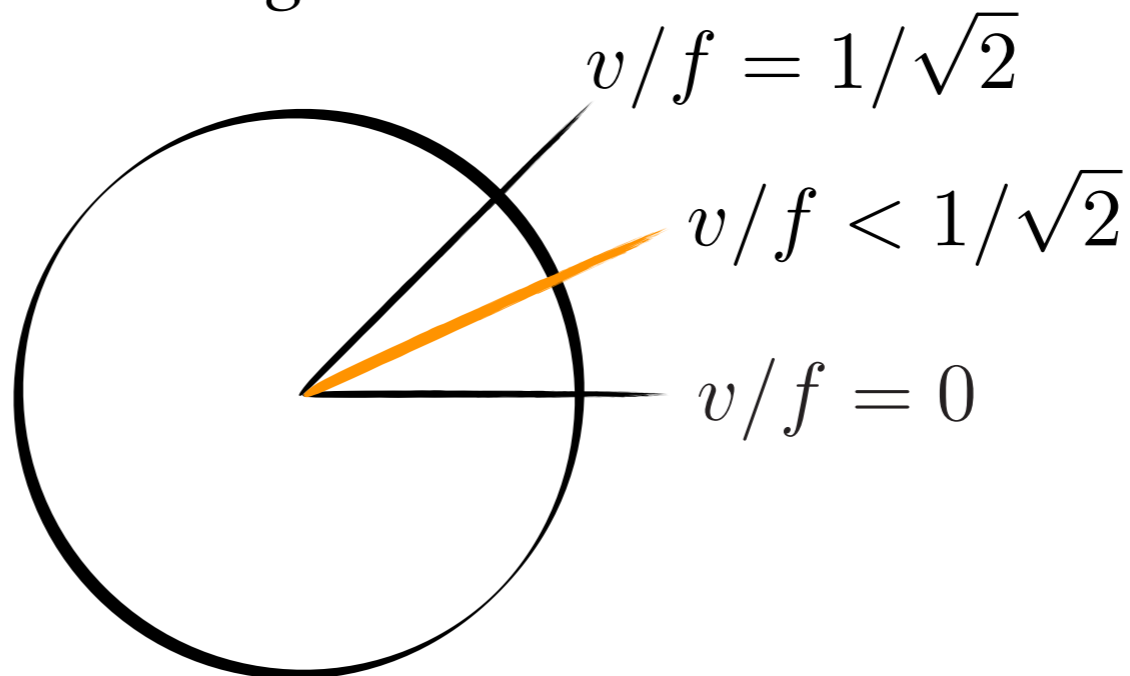
twin Higgs

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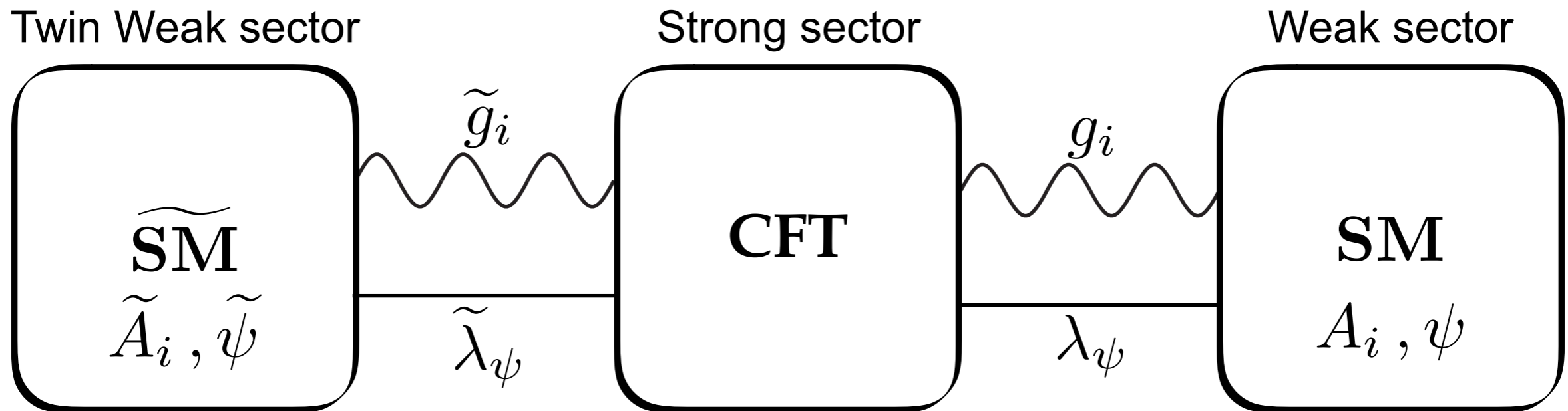
Explicit Z_2 breaking is required to misalign the Higgs VEV, e.g.:

- Twin $U(1)_Y$ is not gauged.
- Only 3rd generations fermions have twins (*fraternal Higgs*).
- Only the top has a twin (*brother Higgs*); see next.

...

composite twin Higgs

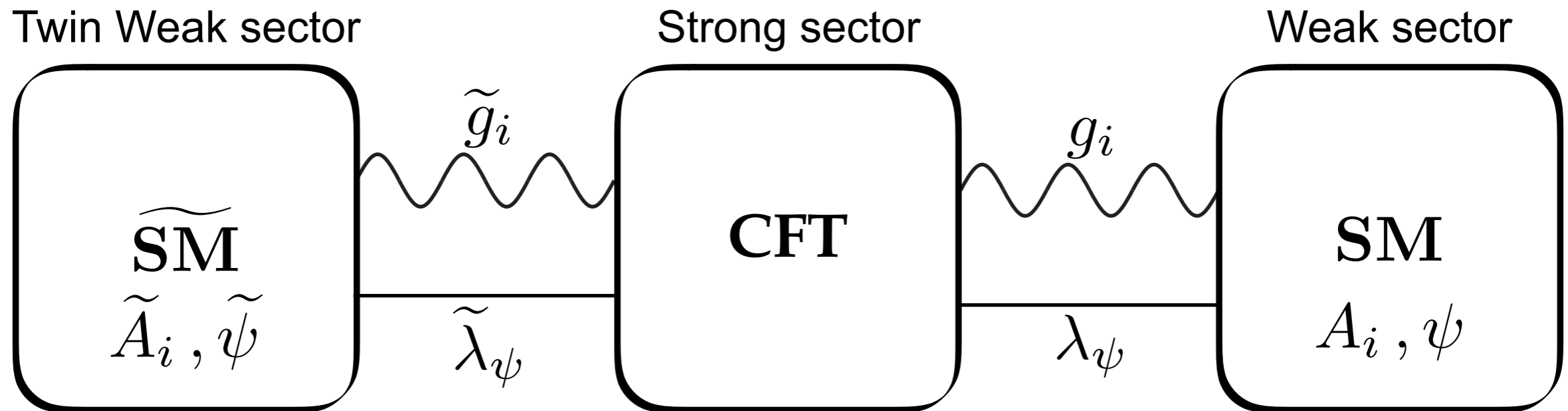
Replace the linear σ -model by strong sector and follow through.



$$[SO(8)/SO(7)] \times SU(3)_C \times \widetilde{SU(3)}_C \times U(1)_X \times \widetilde{U(1)}_X \times Z_2$$

composite twin Higgs

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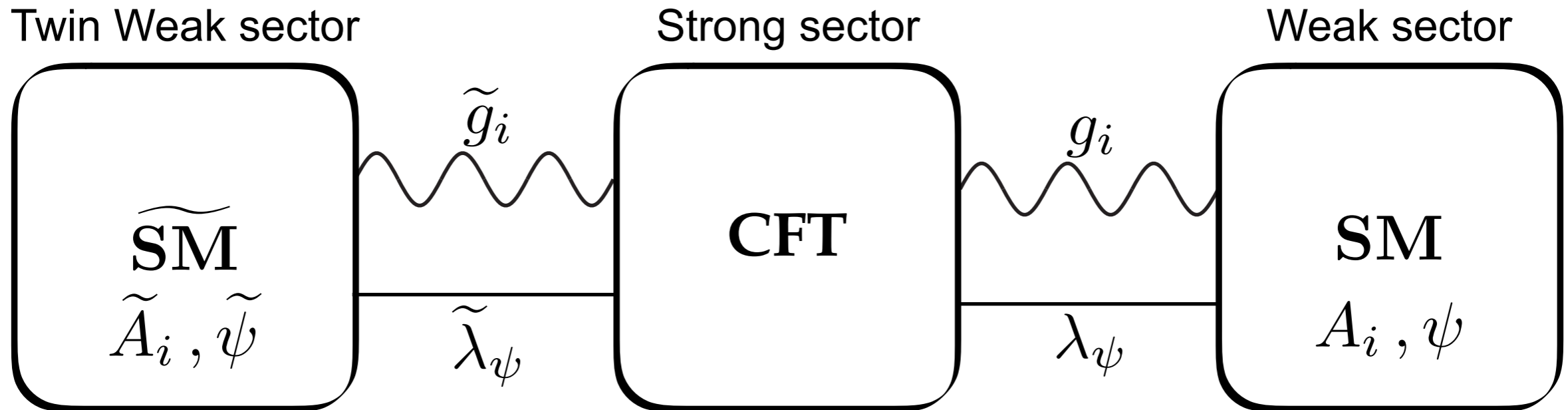
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PC

$$Z_2 : \widetilde{A}_i \leftrightarrow A_i \longleftrightarrow \widetilde{g}_i = g_i$$

composite twin Higgs

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$$\lambda_q q_L \mathcal{O}_q + \lambda_t t_R \mathcal{O}_t$$

$$\mathcal{O}_q = (\mathbf{8}, \mathbf{3}, \mathbf{1})_{2/3,0} \quad \mathcal{O}_t = (\mathbf{1}, \mathbf{3}, \mathbf{1})_{0,2/3}$$

$$\widetilde{\lambda}_q \widetilde{q}_L \widetilde{\mathcal{O}}_q + \widetilde{\lambda}_t \widetilde{t}_R \widetilde{\mathcal{O}}_t$$

$$\widetilde{\mathcal{O}}_q = (\mathbf{8}, \mathbf{1}, \mathbf{3})_{0,2/3} \quad \widetilde{\mathcal{O}}_t = (\mathbf{1}, \mathbf{1}, \mathbf{3})_{0,2/3}$$

$$Z_2: \widetilde{\psi} \leftrightarrow \psi \longleftrightarrow \widetilde{\lambda}_\psi = \lambda_\psi$$

twin Higgs phenomenology

- The Higgs remains a pseudo-NGB:

$$\frac{1}{f^2} (\partial_\mu |H|^2)^2 \quad \text{Higgs couplings} \quad \delta g_h \sim \frac{v^2}{f^2} \lesssim 0.1 \quad f \gtrsim 750 \text{ GeV}$$

- The strong sector has a mass gap naturally high*: $m_* \approx 5 \text{ TeV}$

e.g. S-parameter

$$\hat{S} \sim \frac{m_W^2}{m_*^2} \lesssim 10^{-3}$$

- No production of heavy resonances at the LHC.
- Higgs portal type of collider phenomenology.

Symmetries have shaped the way we address the limitations of the SM.

One may argue that we have taken this philosophy to the extreme, for a good purpose, the *electroweak hierarchy problem*.

Variants of the standard solutions based on symmetries, such as Composite Higgs models, **no** longer require light **colored top partners**.

Searches for these theories are on its way.



DON'T PANIC
ACT NATURAL

try to

Thank you!

light & weakly coupled top partners

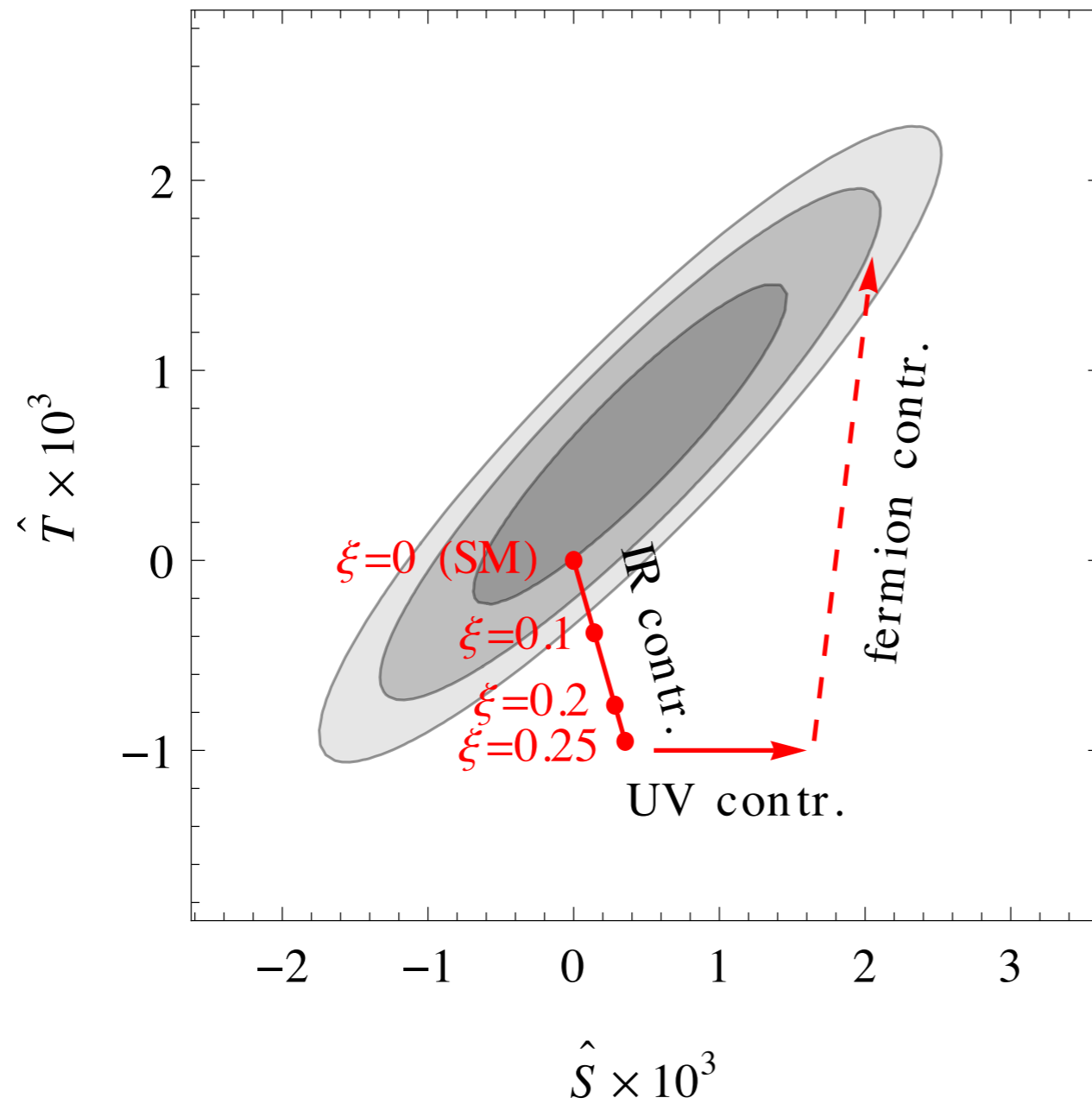
$$m_T < m_* \approx 2.5\text{TeV}$$

S-parameter bound

There might be several reasons, e.g.:

- $\epsilon_{q,t} \rightarrow 1 \iff d(\mathcal{O}_{q,t}) \rightarrow 3/2 = \text{free field dimension}$
- Accidental Ψ chiral symmetry.
- Large N counting.

EWPT & top partners



$$\Delta \hat{T} \sim \frac{3y_L^2}{16\pi^2} \frac{y_L^2 v^2}{m_*^2}$$

Another way to understand twin Higgs:

